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- Initialize each particle  $\vec{x} \in \mathbb{R}^n$  with a random position in the search-space:

$$\vec{x} \sim U(\vec{b}_{lo}, \vec{b}_{up})$$

where  $\vec{b}_{lo}$  and  $\vec{b}_{up}$  are the lower and upper boundaries of the search-space.

- Set each particle's best known position to its initial position:

$$\vec{p} \leftarrow \vec{x}$$

- Initialize each particle's velocity  $\vec{v} \in \mathbb{R}^n$  to random values:

$$\vec{v} \sim U(-\vec{d}, \vec{d})$$

where  $\vec{d} = |\vec{b}_{up} - \vec{b}_{lo}|$

- Initialize the swarm's best known position  $\vec{g}$  to the  $\vec{x}$  for which  $f(\vec{x})$  is lowest.
- Until a termination criterion is met, repeat the following:

- For each particle  $\vec{x}$  in the swarm do the following:

- \* Pick two random numbers:  $r_p, r_g \sim U(0, 1)$
- \* Update the particle's velocity  $\vec{v}$  as follows:

$$\vec{v} \leftarrow \omega \vec{v} + \phi_p r_p (\vec{p} - \vec{x}) + \phi_g r_g (\vec{g} - \vec{x})$$

where  $\omega$ ,  $\phi_p$ , and  $\phi_g$  are user-defined behavioural parameters.

- \* Bound the velocity, that is, for all dimensions  $i$  update  $v_i$ :

$$v_i \leftarrow \text{Bound}(v_i, -d_i, d_i)$$

See figure 2 for the definition of Bound()

- \* Move the particle to its new position by adding its velocity:

$$\vec{x} \leftarrow \vec{x} + \vec{v}$$

- \* Bound the position, that is, for all dimensions  $i$  update  $x_i$ :

$$x_i \leftarrow \text{Bound}(x_i, b_{lo_i}, b_{up_i})$$

- \* If  $(f(\vec{x}) < f(\vec{p}))$  then update the particle's best known position:

$$\vec{p} \leftarrow \vec{x}$$

- \* If  $(f(\vec{x}) < f(\vec{g}))$  then update the swarm's best known position:

$$\vec{g} \leftarrow \vec{x}$$

- Now  $\vec{g}$  holds the best found position in the search-space.
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Figure 1: PSO pseudo-code.