Emergence of dynamic memory traces in cortical microcircuit models through STDP

Abbreviated title: Dynamic memory traces through STDP

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Abstract

Numerous experimental data suggest that simultaneously or sequentially activated assemblies of neurons play a key role in the storage and computational use of long term memory in the brain. But a model which elucidates how these memory traces could emerge through STDP has been missing. We show that stimulus-specific assemblies of neurons emerge automatically through STDP in a simple cortical microcircuit model. The model that we consider is a randomly connected network of well known microcircuit motifs: pyramidal cells with lateral inhibition. We show that the emergent assembly codes for repeatedly occurring spatio-temporal input patterns tend to fire in some loose sequential manner, reminiscent of experimentally observed stereotypical trajectories of network states. We also show that the emergent assembly codes add an important computational capability to standard models for online computations in cortical microcircuits: the capability to integrate information from longterm memory with information from novel spike inputs.

1 Introduction

Neural computations in the brain integrate information from sensory input streams with longterm memory in a seemingly effortless manner. But we do not yet know what mechanisms and architectural features of networks of neurons are responsible for this astounding capability.

It has been conjectured that co-active ensembles of neurons, often referred to as cell assemblies (Hebb, 1949), as well as stereotypical sequences of assemblies or network states play an important role in such computations (Buzsaki, 2010). In fact, a fairly large number of experimental studies from (Abeles, 1991) over (Jones et al., 2007, Luczak et al., 2007, Fujisawa et al., 2008, Pastalkova et al., 2008, Luczak et al., 2009) to (Bathellier et al., 2012, Harvey et al., 2012, Xu et al., 2012) suggest that stereotypical trajectories of network states play an important role in cortical computations. But it is not clear how those assemblies and stereotypical trajectories of network states could emerge through STDP.

There exists already a model for neural computation with transient network states: the liquid state machine, also referred to as liquid computing model (Maass et al., 2002, Haeusler and Maass, 2007, Sussillo et al., 2007, Buonomano and Maass, 2009, Maass, 2010, Hoerzer et al., 2012). Building on preceding work in (Buonomano and Merzenich, 1995) this model shows how important computations can be carried out by experimentally found networks of neurons in the cortex, that consist of diverse types of neurons and synapses (including diverse short term plasticity of different types of synaptic connections), and specific connection probabilities between different populations of neurons (instead of a deterministically constructed circuit). It proposes that temporal integration of incoming information and generic nonlinear mixing of this information (in order to boost the expressive capability of linear readout neurons) are primary computational functions of a cortical microcircuit. A concrete prediction of the model is that transient (“liquid”) sequences of network states integrate information from incoming spike inputs over time spans on the order of a few 100 ms. This prediction has been confirmed by several experimental studies (Nikolic et al., 2009, Bernacchia et al., 2011, Klampfl et al., 2012). However the liquid computing model did not consider consequences of synaptic
plasticity within the microcircuit, and could not reproduce the emergence of longterm memory in the form of assemblies or stereotypical sequences of network states. We show that longterm memory traces automatically emerge in this model if one adds three experimentally supported constraints:

- the fact that pyramidal cells and inhibitory neurons tend to be organized into specific network motifs
- the fact that synapses between pyramidal cells are subject to STDP
- the fact that neural responses are highly variable (“trial-to-trial variability”).

We show that in the resulting biologically more realistic model both assembly codes and stereotypical trajectories of circuit states emerge through STDP for repeatedly occurring spike input patterns. We also provide a theoretical explanation for this, and we demonstrate additional computational capabilities of the resulting new model for online computations with longterm memory in cortical microcircuits.

2 Methods

We first review the traditional liquid computing model, then we describe the modified model that is examined in this article. Afterwards we describe the STDP rule that is applied in this model. Finally we specify the benchmark tasks that are used to evaluate the capability of the model for online computation on new spike inputs in Figure 12, and we provide all technical details of our computer simulations.

2.1 Traditional liquid computing model

The traditional liquid computing model (more formally called liquid state machine) (Maass et al., 2002) is a recurrent network of excitatory and inhibitory spiking neurons (see Figure 1A), with a distance dependent connection probability between any pair of neurons. The temporal dynamics of different neurons and synapses in the model can be diverse and nonlinear, as reported in experimental data on cortical microcircuits. In fact, theoretical results suggest that this diversity supports generic computations in cortical microcircuits (Maass et al., 2002). Two such generic computations (XOR as a typical nonlinear operation, and memory for a preceding spike input) are described below in section 2.4, since they are used in this article to evaluate the performance of our modified liquid computing model on standard liquid computing tasks (see Figure 12). The computational capability of a liquid computing model is commonly tested by training memoryless linear readout neurons (modelling downstream neurons) with the help of a teacher (supervised learning) to approximate the target output of a specific computational task. In previously considered versions of the liquid computing model no specific local connection patterns (such as specific network motifs) were introduced in the network, and no longterm synaptic plasticity was considered within the network. Only the weights to readout neurons were trained, typically by algorithms such as linear regression, or the FORCE algorithm (Sussillo et al., 2007), that did not aim at modelling biological synaptic plasticity. Rather they aimed at measuring how much information the network contained about the target output of a specific computation.

2.2 Modified liquid computing model

Experimental data show that generic cortical microcircuits are not assembled in a random manner from excitatory and inhibitory neurons, like in the traditional liquid computing model.
In particular, as emphasized in (Douglas and Martin, 2004), ensembles of pyramidal cells on superficial and deep layers tend to form through mutual synaptic connections with inhibitory neurons so-called (soft) Winner-Take-All (WTA) circuits, where usually at most one pyramidal cell in the ensemble fires (see Figure 1B). Hence the modified liquid computing model is a recurrent network of WTA circuits (of different sizes (see Figure 1C)). According to (Markov et al., 2011) the probability that two neurons are monosynaptically connected drops exponentially with the distance \(d\) between their somata. In order to mimick this distance-dependent connection probability in our microcircuit model, we arrange its units, the WTA-circuits, on a 2D grid (with each WTA-circuit occupying one grid point). In this paper, the grid size is 10x5 for all networks. Thus, each network consists of 50 WTA circuits. We then create a synaptic connection from an excitatory neuron \(z_k\) to some excitatory neuron \(z'_k\) in two WTA-circuits of distance \(d\) with probability \(p(d)=\exp(-\lambda d)\), according to the data-based rule of (Markov et al., 2011), see Figure 1D. In addition \(z'_k\) receives synaptic inputs from external sources (see Figure 1C). Thus the presynaptic neurons \(y_1, \ldots, y_n\) of a generic excitatory neuron \(z_k\) in some WTA-circuit are neurons in various other WTA-circuits, as well as external input neurons. All of these synaptic connections are subject to short term dynamics and STDP, as described below.

Each WTA circuit in our model consists of some finite number \(K\) of stochastically spiking neurons (\(z_1\) to \(z_K\) in Figure 2A) with lateral inhibition. The number \(K\) is drawn independently for each WTA circuit from a uniform distribution between a pre-defined minimum and maximum number (here: 2-10, and 10-50 in Figure 9). Thus the resulting recurrent network of WTA circuits consists on average of about 300 neurons (1500 in the case of Figure 9). The larger WTA circuits were needed for Figure 9 for the emergence of assemblies with sufficiently long firing pattern.

Each of these neurons \(z_k\) is viewed as a model for a pyramidal neuron, that receives (apart from the lateral inhibition) synaptic inputs from some other pyramidal cells \((y_1, \ldots, y_n)\), see Figure 2A. The membrane potential of neuron \(z_k\) (without the impact of lateral inhibition) is given by

\[
    u_k(t) = \sum_{i=1}^{n} w_{ki} y_i(t) + w_{k0},
\]

where \(y_i(t)\) is the current value of the EPSP from the \(i\)-th presynaptic neuron, which is weighted by the current weight, \(w_{ki}\), of their synaptic connection. \(w_{k0}\) is a bias or excitability parameter of neuron \(k\). Each EPSP is modelled as an alpha shaped kernel with rise time constant \(\tau_{\text{rise}}=2\text{ms}\) and decay time constant \(\tau_{\text{decay}}=20\text{ms}\):

\[
    y_i(t) = \sum_{t_p} e^{\frac{t-t_p}{\tau_{\text{rise}}}} - e^{\frac{t-t_p}{\tau_{\text{decay}}}},
\]

where the sum is over all presynaptic spike times \(t_p\).

Neuron \(z_k\) outputs a Poisson spike train with instantaneous firing rate
\[ r_k(t) = R_{\text{max}} \cdot \frac{e^{u_k(t)}}{\sum_{j=1}^{K} e^{u_j(t)}}. \]  

(3)

Thus it fires with a rate proportional to the exponent of its current membrane potential \( u_k(t) \), normalized by the current total activation of all \( K \) neurons in the WTA circuit, \( \sum_{j=1}^{K} e^{u_j(t)} \). \( R_{\text{max}} \) is the maximum sum of the firing rates of all neurons \( z_1, \ldots, z_K \) in a WTA circuit.

The lateral inhibition of the WTA circuit (Figure 2A) is modelled in an abstract way as the denominator of (3) ("divisive normalization"). One can rewrite equation (3) as

\[ r_k(t) = R_{\text{max}} \cdot \exp[u_k(t) - I(t)], \]

with

\[ I(t) = \log \sum_{j=1}^{K} e^{u_j(t)}, \]

a term that can in principle be approximated by the inhibitory circuit in Figure 2A. We chose here the more abstract implementation of (Nessler et al., 2010, Nessler et al., 2013), where the ratio in (3) can be viewed as a discrete probability distribution over \( \{1, \ldots, K\} \), which at any time determines how the total activity \( R_{\text{max}} \) is spread among the output neurons of a WTA circuit. This abstract way of modelling lateral inhibition has the side-effect that it normalizes the sum of firing rates in the WTA circuit to a fixed value (set to 100 Hz in this paper), even in the absence of external input. We have demonstrated in Figure 6D (where this value was reduced to 70 Hz during those phases where the external input consisted just of noise spikes at a low rate) that this simplification of the model does not affect the effects that we study (emergence of cell assemblies) in a negative manner. Furthermore in other work (Haeusler and Maass, 2013) it is shown that the abstract normalization of (3) can be approximated via connections to and from a pool of inhibitory neurons (as in Figure 2A) that reproduces the experimentally found tracking of excitation through inhibition in cortical microcircuits (Okun and Lampl, 2008).

2.3 Synaptic plasticity

All synaptic connections from external inputs to WTA-circuits and between WTA-circuits are assumed to be subject to short term plasticity and longterm plasticity. It is well-known that biological synapses are not static, and have a complex inherent temporal dynamics (see, e.g., (Markram et al., 1998, Gupta et al., 2000)). More precisely, the amplitude of an EPSP caused by an incoming spike does not only depend on the current synaptic weight, but also on the recent history of input spikes. We modelled this shortterm dynamics of synapses between excitatory neurons in the network like in the traditional liquid computing model of (Maass and Markram, 2002). This model for short term plasticity is based on (Markram et al., 1998), and predicts the amplitude \( A_k \) of the \( k \)-th input spike in a spike train with interspike intervals \( \Delta_1, \Delta_2, \ldots, \Delta_{k-1} \) as

\[ A_k = w_k \cdot u_k \cdot R_k, \]

\[ u_k = U + u_{k-1} (1 - U) \exp(-\Delta_{k-1} / F), \]

\[ R_k = 1 + (R_{k-1} - u_{k-1} R_{k-1} - 1) \exp(-\Delta_{k-1} / D), \]  

(4)

with hidden dynamic variables \( u, R \in [0,1] \) and initial values \( u_1 = U, R_1 = 1 \). The parameters \( U, D, \) and \( F \) in our model were chosen independently for each synapse from Gaussian distributions with means 0.5, 0.11, and 0.005, respectively; the standard deviation was always one half of the
mean, with $y(t)$ defined according to (2). These distributions are based on data for synaptic connection between pyramidal cells according to (Markram et al., 1998), except that the time constants of depression ($D$) and facilitation ($F$) are divided by 10. Since $D \gg F$, these synapses are depressing, i.e., the amplitudes of EPSPs caused by successive spikes are decreasing. The smaller the interspike interval, the stronger is this decrease. In addition, the same synaptic connections are also assumed to be subject to longterm plasticity (STDP). More precisely, the following weight update is applied to the weight $w_{ki}$ of the synaptic input from the $i$-th presynaptic neuron $y_i$ to neuron $z_k$ whenever neuron $z_k$ fires:

$$\Delta w_{ki} = y_i(t) \cdot c \cdot e^{-w_{ki}} - 1,$$

(5)

with $y(t)$ defined by (2). The corresponding STDP curve is shown in Figure 2B. The constant $c$ is chosen so that the weights are kept within the range of positive values. For our simulations we have chosen $c = 0.05 \cdot \exp(5) = 7.42$. This value arises from a learning rate of 0.05 and an offset of 5 for moving all weights into the positive range. If there is a recent preceding spike, the weight change is positive and depends on the current EPSP $y_i(t)$ and on the current weight $w_{ki}$ (in fact, the positive part of the STDP curve has the shape of an EPSP). Whenever there is a postsynaptic spike that is not accompanied by an immediately preceding presynaptic spike of neuron $i$ (i.e., the value of the current EPSP $y_i(t)$ is low), the weight is reduced by a constant amount 1. In this case the firing of neuron $z_k$ is typically caused by preceding firing of other presynaptic neurons $y_j$, leading to an increase of $w_{kj}$ according to the positive part of STDP. The resulting reduction of $w_{ki}$ can therefore be viewed as a qualitative model for the impact of synaptic scaling (Turrigiano, 2008), that might for example arise from a competition for AMPA-receptors within neuron $z_k$, and tends to keep the sums of all weights relatively constant. The excitability of neuron $z_k$ is changed by $\Delta w_{k0} = c \cdot e^{-w_{k0}} - 1$ whenever neuron $z_k$ fires, and by $\Delta w_{k0} = -1$ in every simulation time step ($dt = 1$ ms) where neuron $z_k$ does not fire.

Moreover, all these weight changes are applied with an adaptive learning rate which follows a variance tracking principle (Nessler et al., 2013). Initial values for weights and excitabilities are chosen to be 0.

This form (5) of the STDP learning rule was chosen because it facilitates a theoretical understanding of resulting changes in weights and excitabilities (see (Nessler et al., 2013), (Habenschuss et al., 2013)). More specifically, it supports a theoretical understanding of why STDP drives competing neurons in a WTA circuit to specialize each on a different cluster of (spatial) spike patterns in its high dimensional spike input stream. It is shown in Figure 4 of (Nessler et al., 2013) that the common form of the negative part of the STDP curve appears with this rule (5) if one pairs pre- and postsynaptic spikes at a medium frequency around 20 Hz. Furthermore it is shown in (Nessler et al., 2013), see Figure 8 of that article and the surrounding discussion, that the dependence of weight updates on the current weight in (5) is qualitatively consistent with published experimental data (see also the discussion in section 2.1. of (Habenschuss et al., 2013)). We refer to section 2.3 of (Nessler et al., 2013) for other forms of this dependence that would also be optimal from a theoretical perspective.

In Figure 6 (bottom part of panel A, and panel C) we report the result of a control experiment with a more traditional STDP rule, where the contribution of a pair of a pre- and postsynaptic spike with interval $\Delta t = t_{post} - t_{pre}$ to the weight change is given by
\[ \Delta w_{ki} = c \cdot \begin{cases} A_+(w) \cdot \exp \left( -\frac{\Delta t}{\tau_+} \right) & \Delta t > 0 \\ A_-(w) \cdot \exp \left( \frac{\Delta t}{\tau_-} \right) & \Delta t \leq 0 \end{cases} \]  \hspace{1cm} (6)

We have set here \( A_+(w) = e^{-w_{ki}}, A_-(w) = -1 \), \( \tau_+ = 20\text{ms} \), and \( \tau_- = 60\text{ms} \). Additional zero mean noise was added to each weight update of magnitude \( M \) with standard deviation \( \sigma = 0.3M + 10^{-4} \).

### 2.4 Testing the liquid computing capabilities of the network

We tested the capability of our network to perform nonlinear computations on novel inputs by investigating the performance of a linear readout (trained by linear regression) on two standard benchmark tasks (see Figure 12). The first one was an instance of the binding problem. Consider a network that receives two input streams (Figure 3A). In one input stream a random sequence of spike patterns \( A \) and \( A' \) is presented. The other input stream consists of a random sequence of two other spike patterns \( B \) and \( B' \) (Figure 3B). Both patterns are superimposed by noise spikes (black dots in Figure 3C). The target output is 1 in response to a pattern combination \( A \) and \( B' \) or \( A' \) and \( B \), and 0 in response to a pattern combination \( A \) and \( B \) or \( A' \) and \( B' \). This computation is equivalent to the logical exclusive-OR (XOR) function, which decides whether two input bits are different or not. The equivalence becomes clear when one identifies patterns \( A \), \( B \) each with 0, and patterns \( A' \), \( B' \) each with 1. It is wellknown that the XOR function cannot computed linearly, and can not even be approximated well by a linear function. This XOR function has been used previously to test the nonlinear computation capabilities of a laminar cortical microcircuit model (Haeusler and Maass, 2007). If one uses a linear readout from the network, the nonlinear part of the computation has to be carried out within the network.

Here, the weights of recurrent and input connections were initialized randomly forming a similar distribution as if having been trained with STDP. A linear readout (which received as input the low-pass filtered spike trains of the neurons in the network) was then trained by linear regression every 50ms to decide whether one of the pattern combinations \( \langle A,B' \rangle \) or \( \langle A',B \rangle \) had been present during the last 50ms. This procedure is illustrated in Figure 3C (target “XOR”). The input that was used for training the linear readout consisted of a 50s sequence of spike patterns, which amounts to 1000 training samples for the regression. The size of the test set was 120 samples, drawn from a 6s input sequence that was newly instantiated.

As a measure for the performance of the readout we used the point-biserial correlation coefficient between the analog linear readout and the binary target variable. Figure 3D demonstrates that a linear readout neuron cannot perform the desired nonlinear computation if it directly receives the two input streams (low-pass filtered) as its inputs. If however it is trained on the spike responses of the network, it can achieve a performance above chance level (see the gray bars labeled “network” in Figure 3D). Any correlation value significantly greater than zero indicates non-linear transformations by the network itself (see (Nikolic et al., 2009) for a formal proof).

We tested the temporal integration capability of the network with another standard benchmark task. We trained a further linear readout by linear regression to decode the identity
of the pattern which had been presented in input stream 2 in the interval [-100ms,-50ms], i.e., 50 ms before the current point in time (target “memory” in Figure 3C). The target output was 1 if this earlier input pattern was B’, else 0. Also in this task the readout can perform significantly better on the network output than on the stimulus directly (Figure 3D).

We used these two computational tasks to analyze in Figure 12 how computational performance of the network on novel inputs is degraded through longterm memory traces.

2.5 Computer simulations and data analysis

All simulations, calculations, and data analysis methods were performed in Python using the NumPy and SciPy libraries. Figures were created using Python/Matplotlib and Matlab. The time step of the simulations was chosen to be 1ms.

2.5.1 Determining cell assemblies

When adapting to an input with repeating patterns embedded within a continuous Poisson input stream, the network produced long-term memory traces in the form of transiently active cell assemblies (Figure 4). If different patterns had been embedded into the input stream, different assemblies emerged simultaneously (Figure 5). In order to determine which neurons belonged to an assembly, we used the perievent time histogram (PETH) of all neurons of the network in response to input patterns. The PETH was estimated with bin size 1ms from 100 successive presentations of a given input pattern. In addition, the PETH was smoothed with a 40ms Hamming window for further data analysis. The resulting value $r_i^{\text{PETH}}(t)$ is an observable measure of the temporal activation trace defined by the instantaneous Poisson firing rate of neuron $i$ (3). We defined a neuron $i$ as belonging to a stimulus-induced assembly if $r_i^{\text{PETH}}(t)$ reached a threshold value of 99Hz (80Hz in the experiment with the traditional STDP rule in Figure 6) in at least one simulation step during the duration of the associated input pattern.

2.5.2 Analysis of the sequential activation of neurons

Having determined which neurons belong to an assembly, we ordered them according to their mean activation time during the presentation of an input pattern in order to reveal the stereotypical sequential activation of the memory trace. This mean activation time was calculated as follows. For each neuron $i$, we considered the temporal activity profile during pattern presentations of a particular input pattern, $r_i^{\text{PETH}}(t)$, for $t = 1, \ldots, T_p$, where $T_p$ is the length of the pattern in simulation time steps (e.g., $T_p = 300$ for a pattern duration of 300ms and simulation time step 1ms). We computed the center of mass $t_i^*$ of this temporal activity profile as

$$t_i^* = \frac{T_p}{2\pi} \cdot \arg \left[ \frac{\sum_{t=1}^{T_p} r_i^{\text{PETH}}(t) \exp \left( \frac{tT_p}{2\pi} \right)}{\sum_{t=1}^{T_p} r_i^{\text{PETH}}(t)} \right].$$

In equation (7) we interpret time as the angle in the complex plane and compute the angle of the average complex number, weighted by the activation $r_i^{\text{PETH}}(t)$. In order to analyze
sequential activation of neurons we ordered them according to their values of $t_i^*$. This mean activation time is equivalent to the mean spike latency defined in (Luczak et al., 2009).

2.5.3 Similarity and stereotypy of cell assemblies
We used several criteria to quantify the stability of the emerging cell assemblies. We use the term similarity to specify how reliably the order of activation is maintained across different replays of the same memory trace (in the following called trials). This is measured as Spearman’s rank correlation, which evaluates the correlation between two rank variables. We followed here the procedure from (Luczak et al., 2009) and calculated histograms of rank correlations between the mean activation times on single trials (defined by the mean spike latency, i.e., the average spike time, in this trial) and the mean activation times on the average response over multiple trials (estimated by the PETH and equation (7)). Rank correlation ranges from -1 to +1, values greater than zero indicate that the order of activation is mostly maintained across trials.

On the other hand, we use the term stereotypy to assess how the exact shape of the temporal activation traces of individual neurons are maintained across different trials. This is measured simply as the correlation between the temporal activity trace of a single neuron (defined by its PETH) during two successive trials, averaged over all neurons participating in the assembly.

2.5.4 Determining the onset of spontaneous upstates
In the absence of stimulation the network produces spontaneous activity during which previously learned memory traces are replayed (Figure 7). The onsets of these spontaneous replays can only be determined approximately. Once the neurons participating in the assembly are determined (see above) one can compute the summed activation of the assembly, $r(t) = \sum_i r_i^{PETH}(t)$. We filtered this summed trace with a rectangular window of the expected duration of the memory trace (which is given by the duration of the previously learned patterns $T_p$). We then looked for maxima in this filtered trace that were above a certain threshold. If such a maximum is located at $t'$, then an approximate interval for an upstate was reported as $[t'-T_p/2; t'+T_p/2]$.

3 Results
It is well known that cortical microcircuits are composed of generic network motifs: ensembles of excitatory neurons (pyramidal cells) that are subject to lateral inhibition. (Douglas and Martin, 2004). These network motifs are commonly called Winner-Take-All (WTA) circuits. The power and precision of lateral inhibition among pyramidal cells in superficial and deep layers of cortical columns has been confirmed through a large number of experimental studies (Okun and Lampl, 2008, Ecker et al., 2010, Gentet et al., 2010, Fino and Yuste, 2011, Isaacson and Scanziani, 2011, Packer and Yuste, 2011, Avermann et al., 2012). We investigate in this article models of cortical microcircuits that are structured – in accordance with these data – as networks of WTA circuits (see Figure 1). We show that if one takes also the experimentally observed stochasticity of neural responses into account, then the application of STDP in this model has a rather clear and interesting impact on network dynamics and computations:
longterm memory traces in the form of stereotypical trajectories of network states emerge, and support online computations.

3.1  Emergence of stereotypical trajectories of network states

We consider a generic randomly connected recurrent network of stochastic WTA circuits, in which all synaptic connections between pyramidal cells are subject to STDP (see Figure 1 and Methods). We injected into such network a high-dimensional stream of Poisson spike trains (randomly distributed to the neurons in the network). Initially, the neurons in the network responded in a “chaotic” asynchronous irregular manner without any visible structure (lower left plot of Figure 4A). This network response changed drastically when some spatio-temporal pattern (a “frozen” Poisson spike pattern of 300 ms length, overlayed by random noise in the form of Poisson spikes) was repeatedly embedded into the spike input stream. This noise was actually quite substantial, making up 2/5 of the spikes during a pattern presentation. Nevertheless, after 100 s, the network started to respond to each occurrence of the embedded pattern with structured activity of a specific subset of neurons in the circuit (see lower right panel in Figure 4A). In the terminology of (Buzsaki, 2010) one can describe this phenomenon as the emergence of an assembly code for the repeated input pattern. Furthermore the neurons in this assembly tended to fire in some loose order, creating a stereotypical trajectory of network states for this assembly. This stereotypical network response generalized to compressed and dilated variations of the embedded input pattern (see right panels in Figure 4A).

In order to evaluate quantitatively to what extent the observed sequential firing within the emergent assembly is maintained across different pattern presentations, we computed rank correlations between the mean activation times of responses during individual pattern presentations and those of the average response to the pattern. This is the method that had been proposed in (Luczak et al., 2009) for evaluating to what extent a firing order is preserved. Figure 4C shows that these rank correlations are significantly larger than 0. This indicates that the firing order is mostly preserved across pattern presentations. The distribution of rank correlations in the model is qualitatively similar to those found in cortical microcircuit in vivo in response to sensory stimuli (Luczak et al., 2009).

We then injected in a second experiment two different patterns of the same type (again embedded into noise) into the input stream for the network (see red and green spike patterns in Figure 5). Two different cell assemblies emerged after 50s of simulated biological time, one for each of the two patterns (top two groups in lower panel of Figure 5A). The neurons from these assemblies tended to fire sequentially, and this emergent ordering was maintained across pattern presentations (see Figure 5B to Figure 5E). The third group of neurons (the bottom group in the lower panel of Figure 5A) fired irregularly, with less activity during the presentation of either pattern. Figure 5D shows the average spike response of both assemblies over 100 different pattern presentations. One sees that neurons which responded strongly during presentation of the red pattern tended to be silent during the green pattern, and vice versa. Moreover, for both the red and green pattern the sequential activation of neurons in the corresponding assembly was largely maintained during different presentations of the patterns, as shown by the mostly positive rank correlations in Figure 5E. In order to test whether the emergence of the two input specific cell assemblies could be a result of a specific accidental network topology, we repeated the whole experiment 100 times, each time with a new randomly constructed recurrent network of WTA circuits. For each network we measured the
stereotypy of responses of neurons in the two emerging assemblies by the average correlation between the temporal activity trace of a single neuron during two successive presentations of the same pattern. Figure 5F shows that the stereotypy of each assembly increased with time for both the red and green pattern, reaching a plateau after about 25s of noise-embedded input pattern presentations. On the other hand the correlation of temporal activity traces between pairs of neurons from different emergent assemblies remained low (black trace).

These tests confirm that cortical microcircuit models of the considered structure reliably form two different cell assemblies in response to two different input patterns. This holds in spite of the fact that each stereotypical spike input pattern is superimposed by noise spikes (making up 2/5 of the spikes during a pattern presentation). Hence each assembly is activated by a fairly large cluster of somewhat similar input patterns, rather than by a single precisely repeated input pattern. We also would like to point out that the resulting stereotypical trajectories of network states in these microcircuit models are qualitatively similar to the recently recorded activity patterns in posterior parietal cortex during two types of memory-based behaviours (“left trials” and “right trials”) in (Harvey et al., 2012).

Control experiments (see Figure 6) show that a depressing short term dynamics of synapses and STDP on recurrent connections are necessary for the emergence of stimulus specific assemblies as in Figure 5, whereas STDP on synapses from input neurons and a lower level of network activity in the absence of external input (see Figure 6D) are not. The third panel of Figure 6A and Figure 6B show that if the recurrent network of WTA circuits is required by a single very large WTA circuit, stimulus specific assemblies emerge that fire in a more precise order than in experimental data from cortex (but reminiscent of recordings from area HVC in songbirds). The last panel of Figure 6A, as well as Figure 6C, show that stimulus specific assemblies also emerge with a traditional form of the STDP curve (see equation (6) in Methods).

3.2 Replay of stored memory traces during spontaneous activity

It has been shown that in the absence of sensory input in their spontaneous activity cortical circuits often produce firing patterns that are similar to those observed during sensory stimulation (see e.g. (Luczak et al., 2007, Luczak et al., 2009, Xu et al., 2012) and references therein). We investigated whether a similar effect can be observed in our model. We compared the spontaneous activity of the network discussed in Figure 5A-E before and after learning. Figure 7A shows the spike trains of randomly selected neurons, which are drawn from the same groups as in Figure 5A, during spontaneous activity. Neurons which belong to the two different cell assemblies that have emerged in response to the two input patterns (top two groups in Figure 7A) were spontaneously activated, and fired roughly in the same order as during stimulation with the corresponding input pattern (neurons are ordered according to their mean activation time during previous pattern presentations). Sometimes the sequential activation did not reach all neurons in the assembly. Apart from these randomly initiated firing sequences the neurons in these two assemblies remained relatively silent. The third group of neurons (the bottom group in Figure 7A) fired irregularly, and their rate decreased when one of the two assemblies was spontaneously activated.

Figures 7B and 7C analyze the difference between spontaneous and stimulus induced firing activity of the assemblies in more detail. Figure 7B shows the average firing pattern of one assembly over 100 different spontaneous activations. One can still see a stereotypical firing order in the assembly, which is, according to the right panel in Figure 7C, similar to the generic
firing order induced by external stimulation. But the firing order was less precise across spontaneous activations, and compressed in time (compare Figure 7A with Figure 5A).

These emergent firing properties during spontaneous activity of the microcircuit model are qualitatively similar to the experimental data of (Xu et al., 2012), where stimulus induced sequential firing patterns in primary visual cortex of rat were observed also during spontaneous activity, although with less precision and at a higher speed. This occurred after 100 presentations of a visual stimulus (a moving dot), which is in the same range as the number of preceding presentations of each stimulus in our model (about 75 presentations).

Interestingly, the spontaneous replay of trajectories occurs in our model at a higher speed than during a stimulus-entrained replay (as in Figure 5). This is a commonly observed feature of replay of experience-induced trajectories of network states of neurons in the hippocampus and neocortex (Euston et al., 2007, Ji and Wilson, 2007).

3.3 Interlinking of cell assemblies

It has been proposed that cell assemblies are the basic tokens of the “neural syntax” (Buzsaki, 2010), just like words are the basic tokens of the syntax of language. This theory raises the question whether there are neural mechanisms that are able to concatenate assemblies that are frequently activated one after the other. Our model suggests, that such concatenation could emerge already through STDP, without requiring additional mechanisms such as those discussed in (Buszáki, 2010). In a continuation of the experiment described in Figure 5, we exposed the network to a 100 s input stream where the first type of pattern was always followed immediately by the second type of input pattern. In Figure 8 neurons are sorted according to their mean activation time during the red-green pattern combination in the middle. The resulting firing pattern can be viewed as a “neural sentence” that consists of two concatenated assemblies. Presenting the green pattern alone resulted in activation of the corresponding assembly alone. However, presenting the red pattern triggered the sequential activation of both assemblies (the “neural sentence”), regardless of whether the red pattern was followed by the green pattern or not. This demonstrates that both assemblies had been interlinked through STDP.

3.4 Theoretical foundations of the model

The emergence of stereotypical trajectories of network states in the model can be understood on the basis of two theoretical principles. The first principle is the emergence of sparse neural codes for repeating spatial spike input patterns through STDP in WTA-circuits. The WTA-circuit induces not only a competition for firing in response to an input pattern among its neurons, but also a competition for becoming an “expert” neuron for a repeating input pattern that only fires for this pattern (and for variations of it). This long term consequence of the competition for firing in the presence of STDP is obvious, since only those neurons that fire can adjust their synaptic weights via STDP. This effect has already been known for a long time for competitive Hebbian learning in non-spiking artificial neural networks (Rumelhart and Zipser, 1985). Recently it has been shown that this mechanism also works very well for STDP in a WTA-circuit (Gupta and Long, 2009, Masquelier et al., 2009). In fact, under idealized conditions it approximates the Expectation Maximization (EM) process for fitting the weight vectors of the neurons to frequently occurring input pattern (more precisely, for fitting an implicit generative model to the distribution of spike inputs) (Nessler et al., 2013).
The second theoretical principle concerns the effect of STDP in networks of WTA-circuits. In this case a generic neuron in a WTA-circuit receives not only external input, but also synaptic input from neurons in other (or the same) WTA-circuits. Hence it receives external input in conjunction with the spike response of other neurons in the network, that create a temporal context for the current external input. This effect had already been observed in (Rao and Sejnowski, 2001) in a simpler context. For the case of a single WTA-circuit with complete lateral excitatory connectivity (in addition to the lateral inhibition), this process can under idealized conditions be understood rigorously as emergence of a Hidden Markov Model (HMM). Here each competing neuron becomes an expert for one hidden state of its spike input, so that the resulting sequence of hidden states can explain the temporal structure of the spike input stream (Kappel et al., 2013). For the case of a recurrent network of WTA-circuits of different sizes with biologically realistic sparse connectivity, the network carries out a multi-scale hidden state analysis for the external input stream, where larger WTA-circuits provide a higher resolution for hidden state representations.

Both of these theoretical principles require that there exists substantial noise (trial-to-trial variability) in the network, which is implemented in our model through the stochastic selection of “winners” in the WTA-circuits. Without such variability, the described self-organization could not emerge, because the process would get stuck in the next local optimum of a fitness function.

It is shown in (Kappel et al., 2013) that STDP achieves in this model only an online approximation of the forward-pass of the well-known forward-backward algorithm for HMM learning (see (Bishop, 2006)). This implies that an input pattern that is presented in two different temporal contexts (such as the blue pattern in Figure 9A) may or may not be encoded in the network by a common assembly, i.e. by a common guessed hidden state of the input source. Hence the underlying theory does not guarantee that the blue input pattern is represented by different assemblies, depending on whether it follows the red or green input pattern. Our computer simulations (see Figure 9) show that separate assemblies emerge for the blue pattern in different contexts, but that this differential representation is somewhat unstable (it works only if the blue input pattern is not too long, and if it is a rate pattern rather than a spike order pattern). We conclude that additional learning mechanisms (e.g. reward modulated STDP) are needed to stabilize and extend differential assembly representations for very long common input patterns in different contexts. This hypothesis has an interesting relationship to a detail of the experimental setup and training procedure of (Harvey et al., 2012), see in particular their Supplementary Figure 1. The mouse was trained there to run after two visually distinct initial parts of mazes through a visually neutral part. Different neural assembly responses for this neutral part of the maze (in dependency of the different initial parts of the mazes) emerged after a complex training procedure, where this neutral part of the maze was inserted (and extended) between the initial parts and reward locations in a stepwise process. The subsequent decision (turn left, or turn right, depending on the color of the initial part of the maze) provides there an incentive to represent the neutral part of the maze by different assemblies, depending on the context (i.e., the initial part of the maze). From a theoretical perspective such reward based learning protocol can introduce (through rejection sampling) the full power of HMM learning, where common parts of input sequences are definitely represented by different hidden states if this is beneficial for future decisions (see (Kappel et al., 2013) for further details).

This experiment reveals an interesting difference to the self-organisation property of the model considered in (Liu and Buonomano, 2009), where two different brief initial stimuli
produced on the basis of a suitable learning rule (termed presynaptic scaling) two different stereotypical firing responses, that recruited in either case ALL neurons in the recurrent network. No separate assemblies of neurons emerged in that model for these two different input conditions, in contrast to our model and the experimental data of (Harvey et al., 2012). With regard to experimental data on the dependence of assembly codes on the spatial context of a sensory stimulus we refer to (Itskov et al., 2011). It is an interesting open question whether these data can also be reproduced by our model.

3.5 Liquid computing with longterm memory

The liquid computing model (Maass et al., 2002, Buonomano and Maass, 2009) is an attempt to explain how rather stereotypical cortical microcircuits that consist of diverse types of neurons and (dynamic) synapses with many different time constants could support diverse computational processes in many parts of cortex. It proposes that these microcircuits carry out in particular two generic computational operations: integration of temporally dispersed information from its spike inputs, and nonlinear preprocessing in order to enhance the computational capability of linear readout neurons. In preceding versions of the liquid computing model longterm memory was restricted to the synaptic weights of readout neurons. In contrast, the model presented in this paper allows that any synaptic connection between excitatory neurons in the network (or “liquid”) can acquire longterm memory via STDP. Another innovation is that this model takes experimentally found stereotypical network motifs (WTA-circuits) into account. In this improved liquid computing model repeating external spike inputs generate stereotypical trajectories of network states that also modify the structure of its spontaneous activity.

In order to investigate the resulting computational properties of the model, we repeated an experiment from (Maass et al., 2002), where spoken words were used to generate spike input patterns for the network (Figure 10A, B). We used speech samples from the well-known TI46 dataset (also used by e.g., (Hopfield and Brody, 2000)) which consists of isolated spoken digits. We preprocessed the raw audio samples with a model of the cochlea (Lyon, 1982) and converted the resulting analog cochleagrams (Figure 10A) into spike trains as in (Schrauwen and Campenhout, 2003) (Figure 10B). We used 10 different utterances of digits “one” and “two” of a single speaker. 7 of these utterances were used for training, the remaining 3 utterances were used for testing. We embedded noisy variations of these cochlear spike trains in random order into Poisson spike trains of constant rate. This constituted the spike input to our model, a recurrent network of WTA-circuits with STDP like in the preceding experiments.

In contrast to the results in (Maass et al., 2002) it is no longer necessary to train a readout neuron by a teacher for the classification of different spoken digits. The network learned to detect and discriminate between different digits by an emergent assembly coding: presentation of digits “one” and “two” activated after a short while two different assemblies of neurons. Moreover, this behavior generalized to unseen test utterances. In addition, there were also neurons which were silent during the presentation of either digit, and fired irregularly in the absence of any input pattern. The firing patterns of the two assemblies, which exhibit in this case hardly any specific firing order due to the less prominent temporal structure of the spike input patterns, are very easily separable (see their first principle components in Figure 10D). Hence the neurons in a WTA-circuit of external readout neurons learns autonomously during 100 s to separate and classify the spoken digits (see the firing of neurons 1 and 2 in the spike raster of the 4 neurons of this WTA-readout shown in the third panel of Figure 10C). In
contrast to the classical liquid computing model, in this case no teacher is needed to train a readout neuron to classify the spoken digits. Panel F of Figure 10 shows that the performance of such readout without teacher is very bad before STDP was applied to synapses within the current network (i.e., “training time” = 0), even worse than if applied directly to the input spike trains (red line). But after applying STDP to synapses in the recurrent network the performance of this readout without teacher improves very fast, indicating thereby an important functional property of the emergent stimulus specific assembly codes.

One interesting feature of our model is that it also reproduces a characteristic error that had been observed in the experiments of (Harvey et al., 2012), and which might potentially be typical for trajectory-based computations. (Harvey et al., 2012) observed that the trajectory that is characteristic for the current stimulus jumped occasionally to the trajectory that is characteristic for the other stimulus (see Figure 4f of (Harvey et al., 2012)). This effect also occured in our model, see Figure 10E. The black trajectory shown there (which occurred for the stimulus “one”) jumped after a while to an area of the state space that is usually visited by the trajectory for the stimulus “two”.

Figure 11 illustrates two further computational properties of the modified liquid computing model. If parts of the presented spoken digits were omitted for a duration of 100ms, the corresponding assembly continued to fire, thereby bridging this gap in external information. Furthermore, the network exhibited a new generalization capability. We created novel stimuli by generating spike trains from a pseudo-cochleagram that was obtained by taking the mean of the cochleagrams of two specific utterances, one of digit “one” and one of digit “two” (Figure 11B). As seen in the right panel of Figure 11A, the network responded to the spike patterns corresponding to these “averaged” digits on each trial with one of the two assemblies that had previously emerged in response to spoken words “one” and “two”. This response is qualitatively similar to the experimental data of (Ramos et al., 1976), who had already shown very early that neural responses to novel interpolations between two overtrained stimuli tended to be very similar to the neural responses for one or the other of the two overtrained stimuli.

Finally, we explored the tradeoff between the computational benefits of an untrained network, and a network whose synapses had been subject to STDP during reoccurring input presentations. An untrained network can carry out generic temporal integration (fading memory) and nonlinear preprocessing operations on arbitrary, in particular also on completely novel, input streams very well. Figure 12 shows that this capability is reduced through STDP, when the network develops assemblies that respond to repeating network inputs in a stereotypical manner. Hence our model suggests that it is essential that synaptic plasticity is limited, at least for cortical networks that need to retain the capability to process novel inputs in a flexible manner. Such limitation of synaptic plasticity could for example be implemented in the brain by allowing during any learning episode only a small subset of all synapses to be modified by STDP. Molecular mechanisms of this type have been proposed in (Silva et al., 2009).

4 Discussion

We have shown that STDP on synaptic connections between excitatory neurons causes the emergence of input-specific cell assemblies, provided that there is sufficiently much stochasticity (or trial-to-trial variability) in the network, and excitatory neurons are subject to local lateral inhibition. The resulting network activity in the model is strikingly similar to the experimentally observed stereotypical trajectories of network states in sensory cortices (Jones
et al., 2007, Luczak et al., 2007, Luczak et al., 2009, Bathellier et al., 2012), hippocampus and prefrontal cortex (Fujisawa et al., 2008), and parietal cortex (Harvey et al., 2012). Furthermore stereotypical trajectories of network states emerged in our model after about the same number of input repetitions (100 repeats) as in the experiments of (Xu et al., 2012). Hence our model may help to narrow the gap between network activity of cortical microcircuit models and experimentally observed firing patterns of neurons in the cortex.

The experimentally observed stochasticity of neuronal firing (which is likely to result primarily from stochastic synaptic vesicle release (Isaacson and Walmsley, 1995, Tsodyks and Markram, 1997, Goldman et al., 2002, Branco and Staras, 2009)) in combination with the experimentally observed primarily depressing dynamics of synaptic connections between excitatory neurons (Tsodyks and Markram, 1997, Goldman et al., 2002) are important ingredients of our model. They avoid that the network gets entrained in an almost deterministic stereotypical activity pattern that becomes increasingly independent from external input, and tends to reduce the capability of the network to carry out computations on synaptic inputs from neurons outside of the network. (Izhikevich et al., 2004) had previously shown that synaptic depression alone does not suffice for that. The work of (Liu and Buonomano, 2009) suggests that in addition to stochasticity and depressing synapses also local lateral inhibition is required for the emergence of input-specific assemblies through STDP. However they showed that instead of local lateral inhibition also an additional rule for synaptic plasticity (which they called presynaptic-dependent synaptic scaling) generates stimulus-specific stereotypical firing patterns. These differed from the ones observed in our model insofar, as they recruited every neuron in the network, and each neuron fired exactly once during such firing pattern. Also, the duration of assembly activations adjusted themselves in our model to the time course of external stimuli (see Figure 5A), and were able to cover larger time spans than with the mechanisms investigated in (Liu and Buonomano, 2009). The presynaptic scaling rule of (Liu and Buonomano, 2009) and the heterosynaptic learning rule considered in (Fiete et al., 2010) induce an interesting difference in the self-organization of the network dynamics: They organize all neurons in the network into a linear firing order where a single neuron fires at any moment of time (rather than creating assemblies and sequences of assemblies). These long chains are not dependent on ongoing external inputs, and are somewhat reminiscent of the stereotypical autonomous dynamics of the area HVC in songbirds (see (Fiete et al., 2010) for details).

4.1 Relationship to other models

Synfire chains are a special type of stereotypical trajectory of network states, whose occurrence had been proposed in (Abeles, 1982, 1991). A synfire chain is conceptually rather close to an assembly sequence in the sense of (Buzsaki, 2010). The main difference is that one assumes that the neurons within a single assembly of a synfire chain fire almost simultaneously. This assumption provides a nice explanation for precisely timed firing patterns observed in the prefrontal cortex of monkeys with electrode recordings from a few neurons (Abeles et al., 1993). But possibly the less precisely repeating stereotypical trajectories that emerged in our model (see e.g. Figure 5) also provide a statistically valid explanation of these experimental data.

The possible role of synfire chains and related notions of cell assemblies in cognitive processes and memory had been discussed on a more abstract level also in (Wennekers and Palm, 2009) and (Wennekers and Palm, 2000). The impact of STDP in a recurrent network of
spiking neurons had been analyzed extensively in (Morrison et al., 2007). In the absence of external input the network was found to reach a stable distribution of synaptic weights. But external input induced quite different firing regimes ("synfire explosion") in their model. This difference to our model may result from the inclusion of synaptic dynamics and local lateral inhibition in our model. The important role of lateral inhibition in this context had already been highlighted by (Lazar et al., 2009), although in a more idealized model with synchronized threshold gates instead of asynchronously firing spiking neurons. In that model an STDP-like rule in combination with homeostasis was shown to generate input-specific trajectories of network states. A nice review of a variety of effects of STDP in recurrent networks of spiking neurons is given in (Gilson et al., 2010).

It is an interesting open question whether STDP in our model can also reproduce the emergence of continuous attractors (Samsonovich and McNaughton, 1997) that represent continuous spatial memory.

4.2 Experimentally testable predictions of our model

Monitoring the activity of many neurons in awake animals over several days and weeks, while the animal learns the behavioral significance of specific sensory stimuli, is now becoming possible through imaging of intracellular $Ca^{++}$ traces in identified neurons (Huber et al., 2012). Our model predicts that such learning processes cause the emergence of assemblies and assembly sequences for behaviourally relevant sensory stimuli. Through optogenetic stimulation (see (Stark et al., 2012)) one can in principle also generate artificial spike inputs in a local microcircuit, and our model predicts that this will also cause the emergence of stimulus-specific assemblies and trajectories of network states. Our model also predicts that this effect is abolished through inactivation of inhibitory neurons.

In addition our model predicts (see Figure 11 and 12) that an important tradeoff can be observed in the dynamics of local networks of neurons. At one end of this tradeoff curve one will find networks that can differentially respond to novel stimuli in such a way, that substantial information about these stimuli can be read off from their resulting firing activity (as in (Nikolic et al., 2009, Klampfl et al., 2012)). At the other end of the tradeoff curve one will find network responses as discussed in Figure 11, that are more stereotypical and contain primarily information on how similar the current stimulus is to some specific familiar stimulus. We propose, that microcircuits in different parts of the brain operate at different positions on this tradeoff curve. Furthermore, development and extended learning periods are likely to move at least some of these microcircuits into the more stereotypical regime on the right-hand side of Figure 12. A shift towards more stereotypical trajectories of network states as a result of learning had already been observed in (Ohl et al., 2001).

4.3 Summary

Altogether the model for learning in cortical microcircuits that we have presented is a simple extension of the liquid computing model. Whereas the original version of the model (Maass et al., 2002) was only able to model online processing of novel stimuli in a “naïve” network, the here presented extension addresses also the formation and computational use of longterm memory traces. Furthermore, in the original version one had to rely on the contribution of readout neurons (that had to be trained by a teacher) for arriving at a result of a computation (e.g., a classification). The emergence of stimulus-specific assemblies in the extended model makes such external contributions unnecessary (see Figure 10F). Our model provides a
platform for investigating the functional role of assemblies and assembly sequences as potential building blocks for "neural sentences", that may underlie higher brain functions such as reasoning (Buzsaki, 2010). At the same time our model is consistent with many experimental data on synaptic plasticity and the anatomy and physiology of cortical microcircuits.
References


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Figure 1
Figure 1: Traditional and modified liquid computing model. (A) Traditional liquid computing model. (B) More structured generic microcircuit model from (Douglas and Martin, 2004): a recurrent network of WTA-circuits on superficial and deep layers. (C) Resulting modified liquid computing model: A recurrent network of WTA-circuits. Each WTA-circuit is assumed to be positioned on a grid point of a 2D grid, in order to define a spatial distance between them. Each WTA circuit consists of some randomly drawn number K of stochastically spiking excitatory neurons $z_k$ that are subject to lateral inhibition. WTA circuits within the network receive spike inputs from randomly selected excitatory neurons in other WTA circuits in the network, and from the external input to the network. We will focus in section 3.5 (see Figure 10) on WTA-circuits as readouts that do not require a teacher for learning (linear readouts trained by linear regression with the help of a teacher, like in the traditional liquid computing model, are only considered for control experiments in Figure 12). (D) Smooth line shows the distance dependent connection probability $\lambda \exp (-\lambda d)$ between any two excitatory neurons in two WTA-circuits at distance $d$. A histogram of resulting connections for a typical network is also shown.
Figure 2
**Figure 2:** (A) Scheme of the microcircuit motif (WTA-circuit) that is considered. (B) The STDP learning window corresponding to the learning rule (5).
Figure 3
**Figure 3:** The network inherits major generic processing capabilities of the liquid computing model, as shown in Figure 12. (A) In the exclusive-OR (XOR) task a readout neuron has to decide whether specific combinations of input patterns are currently presented to the network. It should respond strongly if pattern A at input stream 1 is accompanied by pattern B’ in stream 2 or pattern A’ by pattern B, but not respond for other combinations of the same patterns. (B) Samples of the four spike patterns A, A’, B, and B’. Each pattern has 50ms duration and consists of Poisson spike trains at 5Hz. (C) Sample stimulus sequence with the patterns shown in B. During simulation 2Hz Poisson spike trains are overlaid as noise (black spikes). In the XOR task the readout should respond only if one of the desired pattern combinations is currently present at the input (indicated by blue rectangles). In a separate memory task the readout should decode the identity of the pattern presented during the interval [-100ms,-50ms] in stream 2 (magenta rectangles). (D) Performance of a linear regression readout for both tasks, trained on the low-pass filtered spike trains of both the network and the stimulus directly (time constant 20ms). The readout was trained to decode the target bit every 50ms, at the end of each pattern (training set 50s/1000 patterns); shown is the performance on a test set (6s/120 patterns), averaged over 100 runs with different patterns and networks (error bars show SD). Performance is evaluated as the point-biserial correlation coefficient between the binary target variable and the analog output of the linear regression.
Figure 4

A. Emergence of cell assemblies in response to a repeating input pattern

B. Neuron activation during pattern

C. Similarity of assembly activations

D. Neuron activation during pattern
Figure 4: The cortical microcircuit model forms a memory trace in the form of a sequentially activated assembly of neurons for a reoccurring sub-pattern within its high dimensional input stream. (A) Top panels: The stimulus consisted of 100 Poisson spike trains of a constant rate (5Hz), into which a frozen Poisson spike pattern at 3Hz was embedded in random intervals (red spikes in top left panel). New 2Hz Poisson spike trains (black spikes) were superimposed over each pattern presentation. The original pattern had 300ms duration. During testing pattern presentations were time warped with a random factor between 0.5 and 2 (top right panel). Bottom panels: Response of the network to test stimuli shown above before (left) and after (right) 100s of applying STDP within the network for such input stream (that contained about 150 pattern presentations). Shown is the activity of 20 randomly selected neurons. To illustrate the sequential activation during pattern presentations, neurons that now respond primarily to this pattern are sorted according to their mean activation time during the pattern (see B). (B) Average activation of the neurons in the emergent assembly during 100 pattern presentations. Neurons are sorted by their mean activation time (white dots) defined as the center of mass of their temporal activity profiles. (C) Histogram of rank correlations between mean activation times for individual pattern presentations and for the average response in B. Most correlations are greater than zero, indicating that the sequence of activations is mostly preserved across pattern presentations. (D) The response to the pattern is unaffected if during training it is sometimes preceded by one of two other Poisson spike patterns of the same length. Shown is the average activation of the neurons (as in B) for an experiment where 10% of the presentations were preceded by pattern 1, and another 10% by pattern 2. It is interesting to compare this result with Figure 9, where the emergence of different assemblies for the same input pattern is demonstrated if it regularly occurs in two different temporal contexts.
Emergence of different cell assemblies in response to two repeating input patterns

Figure 5
**Figure 5:** Two different cell assemblies emerged when two different input patterns occurred repeatedly (embedded into noise). (A) Top panel: The input consisted of 100 Poisson spike trains of a constant rate (5Hz), as in Figure 4, but with two different spike patterns embedded (red and green spikes). The patterns were presented in random order and in random intervals within the noise input. During testing the pattern presentations were time warped with a random factor between 0.5 and 2. Bottom panel: Different cell assemblies emerged for the two patterns (assembly 1 and assembly 2). The response of 20 randomly selected neurons of the network to test stimuli is shown after 50s of pattern presentations (about 75 presentations of both patterns in total). To illustrate the sequential activation during pattern presentations, neurons are sorted according to their mean activation time during the pattern (as in D). (B) Two successive replays of the two assemblies in response to the corresponding input patterns are shown (“Trial #1” and “Trial #2”). Responses for more repetitions of the corresponding input patterns are shown for the neurons with colored pikes in C. (C) Raster plots showing spike times for 4 sample neurons (“n. #1” to “n. #4”) during 20 pattern presentations. Neurons (spikes) are colored as in B. Overlaid traces are PETHs calculated from 100 trials. (D) Average activation of the neurons participating in one of the two assemblies during either of the two patterns. The average is taken over 100 corresponding pattern presentations. Neurons are sorted by their mean activation time (white dots) defined as the center of mass of their temporal activity profiles. (E) Histogram of rank correlations between mean activation times for individual pattern presentations and average activation times according to D. Most correlations are greater than zero, indicating that the sequence of activations is mostly preserved across corresponding pattern presentations. (F) Temporal evolution of the emergence of input specific assemblies is measured by the average correlation between the temporal activity trace of a single neuron in an assembly (averaged over all these neurons) during two successive presentations of the same pattern (red or green, denoted by the corresponding color). The black trace shows the average correlation between activity traces of these neurons for different input patterns (same trace is shown in both panels). All values were averaged over 100 trials with different input patterns and networks (error bars show SD).
Figure 6
Figure 6: Consequences of changes in the network structure or the STDP rule. A number of control experiments elucidate the relevance of specific features of the network model. The base experimental setup is the same as in Figure 5. (A) Responses to the same stimulus (top) are shown after 50s of pattern presentations in the input stream for different variations of the network (panels as in Fig. 5A). From top to bottom: STDP is not applied to recurrent connections, instead their weights remain fixed at random values; the network is composed of a single WTA circuit of comparable size and total activity (268 neurons, $R_{max} = 2500$Hz); input weights remain fixed at random values; temporal dynamics of synapses (paired pulse depression) is deactivated ($R_k = u_k = 1$); another STDP rule was applied (see Methods). (B, C) Histograms of rank correlations as in Fig. 5E for the "single WTA circuit" and "different STDP rule" scenarios. (D) Emergence of assembly codes (similarly as in Figure 5) for a different regulation of network activity: Here the input rate is decreased to 2Hz between input patterns, and the sum of firing rates in the network (spontaneous activity) is reduced from 100 to 70 Hz during this time (by regulating the factor $R_{max}$ for divisive normalization accordingly, see equation (Fehler! Verweisquelle konnte nicht gefunden werden.)). Altogether these control experiments show that short term dynamics (depression) and STDP on recurrent synaptic connections are essential for the emergence of stimulus specific assemblies, whereas STDP on synaptic connection from input neurons, the precise shape of the STDP curve, and a lower level of spontaneous firing are not. If the network of WTA circuits is replaced by a single very large STDP (third panel in A, and B), stimulus specific assemblies also emerge, but their firing order is extremely precise (differing in this respect from most experimental data).
Effect of learning on spontaneous activity

Figure 7
Figure 7: Change in the structure of spontaneous activity through learning. (A) Left: Response of 40 randomly selected neurons of the network to noise input before learning. Right: Response of the same 40 neurons to noise input after 50s of adaptation to an input consisting of two embedded spike patterns (as in Figure 5). Neurons in the two assemblies are sorted according to their mean activation time during preceding pattern presentations (assembly 1/2 and horizontal dotted lines as in Figure 5A). (B) Average activation of the neurons in the top group in A over 100 spontaneous assembly activations. Neurons are sorted by their mean activation time (white dots) defined as the center of mass of their temporal activity profiles. (C) Histogram of rank correlations between the activation times of individual spontaneous assembly activations and the average spontaneous and stimulated activations, respectively. Most correlations are greater than zero, indicating that the sequence of activations is mostly preserved, and similar to the stimulus evoked activation pattern.
Interlinking of cell assemblies

Figure 8
**Figure 8:** Interlinking of cell assemblies. (Top) The red and green pattern (defined and superimposed by noise as in Figure 5) had been shown in immediate succession for 100s (about 125 presentations) in the input stream. This caused the emergence of interlinked assemblies of neurons. While the network responded to the green pattern alone with assembly 2, the red pattern always triggered the whole assembly sequence (assembly 1 followed by assembly 2), regardless of whether it was followed by the green pattern or not. (Bottom) Response of the network to the test input. Shown is the activity of 20 randomly selected neurons. To illustrate the sequential activation during pattern presentations, neurons are sorted according to their mean activation time during the red-green pattern sequence.
A

stimulus
100 neurons

network
assembly 1
assembly 2

50 random neurons

0 0.2 0.4 0.6 0.8 1.0

0.1 0.2 0.3 0.4 0.5 0.6 0.7 0.8 0.9 1.0

stimulus network

B

red context
green context

assembly 1
assembly 2

0 300 time [ms]

C

Similarity of assemblies
assembly 1
assembly 2

Similarity of assemblies
assembly 1
assembly 2

0 40 trials

-0.2 0.2 0.6

rank correlation

-0.2 0.2 0.6

rank correlation

Figure 9
Figure 9: Response to the same input pattern in different temporal contexts. (A) Top: A 200 ms long firing rate pattern (blue) was presented during training and testing in two different contexts, each represented by a preceding 100 ms long rate patterns (red or green). Each input pattern is characterized by a random subset of 10 input neurons that fire with 50Hz, while the other input neurons fire with 1Hz; for each trial new Poisson spike trains are drawn. Bottom: Two different assemblies emerge for the blue pattern: a separate one for each context. (B), (C). Same analysis of network responses during testing as in Figure 5D, E. The two assemblies are activated during test trials in a rather stereotypical firing order, similarly as in 5D, E, although there is here no fixed firing order of input neurons within input patterns. The response of the two assemblies tends to become somewhat unstable towards the end of the 300 ms long input patterns (see A and B). This time point where the input pattern becomes identical (blue pattern) is marked by a dashed black line in panel B.
Emergence of cell assemblies in response to spoken digits

Figure 10
Figure 10: Formation of cell assemblies to different spoken digits. (A) Sample cochleagrams of one specific utterance of each of the digits “one” and “two”. Each cochleagram consists of a 86-dimensional analog trace. (B) Spike trains generated from the cochleagrams in A, equally distributed over 100 neurons. (C) From top to bottom: test stimulus, network response, output of a readout WTA circuit (learning in a completely unsupervised manner), and output of a linear readout trained by linear regression (supervised learning). The test stimulus consisted of 100 Poisson spike trains of a constant rate of 5Hz, into which utterances of digits “one” (red spikes) and “two” (green spikes) of a single speaker were embedded at random time points. These utterances had not been used for training. Resulting spike input patterns were superimposed by 2Hz Poisson spike trains as noise (black spikes). The network response after adapting to such input stream for 100s (about 150 presentations in total of both patterns) shows that different cell assemblies were activated during the presentation of different digits. Shown is the activity of 20 randomly selected neurons. The WTA readout consisted of 4 neurons, whose spike trains are shown. Its synaptic weights resulted from STDP applied during 10s of spoken word presentations after the assemblies in the network had emerged (without a teacher). (D) 3D plot of the first three principal components of the network states during the test phase shown in C. Colors as in C (red: digit “one”, green: digit “two”; responses to intermediate noise not shown). The thick colored lines show the average response over multiple trials, numbers show time in ms after trajectory onset, marked by black dots. (E) Network trajectory for an error trial shown in black (red and green curves are average responses for the two different stimuli as in D). The trajectory started out in the standard way for digit "one", but jumped later to the area of the state space typically visited for digit "two". (F) Evolution of the performance of the unsupervised WTA readout. After every 5s of training of the recurrent network, the WTA readout was exposed for 10s to the spike trains generated by the recurrent network. The resulting performance was measured by the mutual information between the stimulus class (digit) which the recurrent network received as input, and the average firing rates of the neurons in the WTA readout during pattern presentations. Performance was averaged over 100 trials with different networks. Error bars denote SEM. After the recurrent network had received these inputs, the emergent assemblies enabled the WTA readout to achieve a better discrimination than when applied in the same manner directly on the input (stimulus) to the recurrent network (red curve in panel F).
A

Computations with cell assemblies

Network response for interrupted input

Assembly recall for new stimuli

B

spoken digit “one”  spoken digit “two”  superposition  new stimulus

Figure 11
**Figure 11:** New computational properties of the network from Figure 10 (A) Left: The emergent assemblies continued to be activated when the presentation of spoken digits was interrupted during the interval from 100ms to 200ms after pattern onset (indicated by gray shading). Right: The presentation of new patterns (magenta spikes, see B) triggered the activation of one of the two assemblies. (B) The new patterns in A were generated by superimposing the cochleagrams of two utterances, one of digit “one” and one of digit “two”. Cochleagrams were first subsampled to be of equal length (the longer of the two utterances).
Trade-off between liquid computing and assembly formation

Figure 12
Figure 12: Trade-off between generic computational capabilities of a network and the formation of assemblies and stereotypical trajectories of network states in response to repeated input patterns. A standard method for testing the generic nonlinear computational capabilities of a network (XOR) task and its (fading) memory for novel spike inputs was applied (see Methods). The performance of linear readouts trained by linear regression for both tasks were evaluated during test phases after every 5s of adapting to the spike input pattern from Figure 4. This performance decreased as the network adapted through STDP to the repeated input pattern and formed an assembly with a stereotypical trajectory of network states. The stereotypy of this trajectory was measured by the average correlation between the temporal activity trace of a single neuron in the assembly during two successive pattern presentations (averaged over all neurons in the assembly). All performance values were averaged over 100 runs with different patterns and networks (error bars show standard error).